Facile 1,3- and 1,5-Chlorine Migration

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High-level ab initio molecular orbital calculations, using the G2(MP2,SVP) theory (and semiempirical methods) have been used to examine several 1,3- and 1,5-chlorine migrations. It is found that the interaction of chlorine lone pair electrons with a low-lying LUMO accelerates the Cl shift dramatically (lone pair-LUMO-mediated pericyclic reaction). The activation barriers for the 1,3 migration in chloro oxo ketene 1 (Cl(C=O)CH=C=O) and the 1,5-migration in (2-(chlorocarbonyl)vinyl)ketene **2** (Cl(C=O)CH=CHCH=C=O) are only 53 and 61 kJ mol⁻¹, respectively, compared to the 216 and 173 kJ mol⁻¹ barriers for the corresponding unassisted 1,3- and 1,5-sigmatropic shifts of Cl in 3-chloro-1-propene and 5-chloro-1,3-pentadiene. The transition structures for **1** and **2** reveal that migration of the chlorine atoms takes place in the molecular planes. The 1,5-chlorine shift in 6-chlorocyclohexa-2,4-dienone (**3**) has a significantly higher barrier due to a lack of appropriate orbital interaction. The related 1,3-shift in the (chlorocarbonyl)imine $-\alpha$ -chloro isocyanate system is also dramatically accelerated compared with conventional pericyclic 1,3-Cl migration.

Introduction

Interest in the study of concerted processes in organic chemistry has increased markedly since the development of the general theory of orbital symmetry by Woodward and Hoffmann.¹ Thermal and photochemical [1,*n*] sigmatropic rearrangement is one of the more fascinating of these processes, and it has been the subject of several reviews.² Not only carbon and hydrogen migrations, but also shifts of other functionalities including halogen atoms have been documented.3

Although numerous examples of experimental and some semiempirical studies on the migrations of chlorine, 4 bromine, 5 and iodine 6 appeared in the literature, to date there has been a lack of high-level ab initio investigation. In particular, the 1,5-sigmatropic rearrangement of chlorine is a well-explored reaction. Both NMR and semiempirically determined energy barriers have been reported, lying between 110 and 140 kJ $mol⁻¹.^{4b-d}$

Further motivation for the current paper resulted from ongoing studies of the thermal oxoketene-oxoketene rearrangement, which involves a 1,3-shift (eq 1).7 Both experimental⁸ and theoretical⁹ investigations have shown

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that the rate of the 1,3-migration is strongly dependent on the nature of the substituent R.

In particular, the electron-rich *n*-donating methylthio and dimethylamino groups are found to dramatically accelerate this rearrangement. The stabilizing effect of the electron-rich substituents was rationalized in terms of the favorable donor-acceptor interaction between the group R and the vacant central carbon p orbital of the ketene LUMO in the molecular plane (Figure 1). Since halogens possess unshared pairs of electrons, 1,3-halogen migrations in α -oxo ketenes are also expected to be favorable processes (eq 1, $R = Cl$). One may further extend this idea of donor-acceptor interaction to the vinylogous 1,5 shift depicted in eq 2.

We have examined the 1,3- and 1,5-shifts of Cl (eqs 1 and 2; $R = Cl$) by high-level ab initio and semiempirical calculations. In addition, the out-of-plane 1,5-Cl migration in chlorocyclohexadienones^{4b} (eq 4) and the $1,\overline{3}$ -Cl migration in chloromethyl isocyanate¹⁰ (eq 5) are studied.

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Figure 1. Lone pair-LUMO interaction involved in the 1,3-R shift of α -oxoketenes (eq 1).

The reactions are compared with the conventional pericyclic 1,3- and 1,5-shifts of Cl in 3-chloropropene and 5-chloro-1,3-pentadiene.

Computational Methods

Standard ab initio molecular orbital calculations¹¹ were carried out with the GAUSSIAN 94 system of programs.12 The structures and energies of compounds **1**-**3** and related structures were examined at the G2(MP2,SVP) level of theory.13 This corresponds effectively to $QCISD(T)/6-311+G(3df,2p)/l$ MP2/6-31G* energies together with zero-point vibrational and isogyric corrections. In the G2(MP2,SVP) theory, the basisset extension energy contribution is calculated at the MP2 level and the QCISD(T) energy is evaluated using the 6-31G* basis set. It has been shown that the accuracy of the G2(MP2, SVP) method is comparable to that of the G2(MP2)¹⁴ theory but $computationally$ more efficient.¹³ The frozen-core approximation was employed for all correlated calculations. Semiempirical calculations at the AM115 and PM316 levels were performed using MOPAC 6/PC.¹⁷ Calculated geometries and absolute and relative energies are summarized in Tables 1 and 2.

Discussion

1,3-Shift. In general, α -oxo ketenes can exist as a mixture of two conformers: *s-trans* (**1a**) and *s-cis* (**1b**). Our calculations reveal a slight preference for the *s-trans* isomer **1a** by 4.2 kJ mol⁻¹.¹⁸

The transition state for the 1,3-Cl migration $1a \rightleftarrows 1a'$ **(TS1**, Figure 2) is predicted to lie 53 kJ mol⁻¹ above the *s-trans* oxoketene. This calculated barrier is significantly

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Table 1. Calculated (MP2/6-31G*) Structural Parameters for Equilibrium and Transition Structures*^a*

parameter	TS1	$1a$ (s-trans)	$1b$ (s-cis)	
$C1-C1$	2.207	2.904	3.937	
$C3-C1$	2.207	1.813	1.791	
$C1=0$	1.177	1.169	1.169	
$C3=0$	1.177	1.205	1.210	
$C1-C2$	1.383	1.339	1.339	
$C2-C3$	1.383	1.445	1.449	
$O = C1 - C2$	149.4	178.2	180.0	
$O = C3 - C2$	149.4	126.3	127.3	
$C2-C3-C1$	92.6	113.1	111.5	
$Cl-C3-C2-C1$	$\mathbf{0}$	0	180	
$O = C3 - C2 - C1$	180	180	0	
parameter	TS ₃	2a	2 _b	
$C1-C1$	2.123	2.825	4.713	
$C5-Cl$	2.123	1.810	1.779	
$C1=O$	1.185	1.173	1.172	
$C1-C2$	1.393	1.342	1.358	
$C2-C3$	1.390	1.437	1.420	
$C3-C4$	1.390	1.363	1.369	
$C4-C5$	1.393	1.451	1.428	
$O = C1 - C2$	142.0	169.3	162.3	
$O = C5 - C4$	142.0	125.4	125.4	
$Cl-C5-C4$	106.5	115.7	115.3	
$Cl-C5=O$	111.5	118.9	119.4	
$Cl-C5-C4-C3$	0	$\bf{0}$	180	
$O=C1-C2-C3$	180	180	180	
$O = C5 - C4 - C3$	180	180	0	
parameter		TS ₆	3a	
$C1-C1$	2.483	2.685		
$C2-C1$	2.467	1.812		
$C1=0$	1.230	1.231		
$C1-C2$		1.482	1.531	
$C2-C3$		1.390	1.467	
$C3-C4$		1.400	1.355	
$C4-C5$		1.400	1.459	
$C5-C6$		1.390	1.349	
$C6-C1$		1.482	1.491	
$C2-C1-C6$		111.0	117.1	
$C1-C2-C3$		118.2	115.1	
$O = C1 - C2 - C3$		-140.6	-157.8	
$Cl-C1-C2-C3$		100.3	120.6	

^a Bond lengths in Å and bond angles in deg.

less than that for the 1,3-H shift in formylketene (144 kJ mol⁻¹) but comparable to those for the amino (71 kJ mol⁻¹) and thio (47 kJ mol⁻¹) substituents.^{9b} Therefore, chlorine is also an excellent migrating group. This is readily explained in terms of the lone pair-LUMO interaction shown in Figure 1. Thus, we predict 1,3-Cl migration in α -oxo ketenes to be an observable process. We are currently investigating the scope of such rearrangements experimentally.

In contrast to the very facile Cl migration in α -oxo ketenes, the calculation of the activation energy for the corresponding 1,3-Cl shift in 3-chloro-1-propene reveals a barrier of 216 kJ mol⁻¹ and an out-of-plane transition state (**TS2**, Figure 2), thereby demonstrating the importance of the above-mentioned ketene orbitals.

1,5-Shift. In order to compare the 1,3-Cl shift in α -oxo ketene with a possible 1,5-shift, we have chosen the vinylogous (2-(chlorocarbonyl)vinyl)ketene (**2**), which should give a planar six-membered transition state for the 1,5-Cl migration. However, the additional ethenyl group leads to an increased number of conformers. We have considered all possible conformers of **2** with respect to single and double bond isomerizations, resulting in a total of eight conformers.

2b is calculated to be the most stable conformer. **2e**-**2h** lie within 4 kJ mol-¹ of **2b**, while **2c** and **2d** are about

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Table 2. Calculated Total and Relative Energies

absolute energies			relative energies			
species	G ₂ (MP ₂ , SVP)	AM1	PM ₃	G ₂ (MP ₂ , SVP)	AM1	PM ₃
	(hartrees)	$(kJ \text{ mol}^{-1})$	$(kJ \text{ mol}^{-1})$	$(kJ \text{ mol}^{-1})$	$(kJ \text{ mol}^{-1})$	$(kJ \text{ mol}^{-1})$
1a	-724.70234	-200.4	-226.6	0.0	0.0	1.0
1b	-724.70074	-201.8	-233.6	4.2	-1.3	-7.0
TS1	-724.68228	-112.1	-175.6	52.7	88.3	51.0
2a	-801.93722	-118.4	-131.9	28.9	23.9	21.3
2 _b	-801.94822	-142.3	-153.2	0.0	0.0	0.0
2с	-801.94465	-140.0	-162.5	9.4	2.3	-9.3
2d	-801.94454	-143.8	-164.8	9.6	-1.5	-11.6
2e	-801.94672	-127.2	-132.0	3.9	15.1	21.2
2f	-801.94767	-141.8	-158.6	1.4	0.5	-5.4
$\frac{2g}{2h}$	-801.94705	-139.8	-162.9	3.1	2.5	-9.7
TS ₃ 3a	-801.94687 -801.92490 -766.03265	-143.6 -69.4 -44.7	-165.3 -109.9 -47.3	3.5 61.2 0.0	-1.3 72.9 0.0	-12.1 43.3 0.0
TS ₅	-765.98673	145.4	108.1	120.6	190.1	155.4
4a	-666.79077	-57.3	-86.2	0.0	0.0	0.0
4b	-666.80725	-80.8	-89.1	-43.3	-23.5	-2.9
TS6	-666.74015	104.4	51.5	132.9	161.7	137.7

10 kJ mol-¹ higher in energy (Table 2). Structure **2a**, preorientated for the 1,5-chlorine shift, is found to be 29 kJ mol⁻¹ higher in energy.

The 1,5-Cl migration in **2a**, which is orientated favorably for the 1,5-shift, is predicted to have an activation barrier of 32 kJ mol⁻¹, via the planar six-membered ring transition structure **TS3** (Figure 3). The overall activation barrier for conformer **2b**, the most stable conformer, is therefore 61 kJ mol⁻¹. Hence, 1,5-Cl migration in 2 is predicted to be even more facile but comparable with the 1,3-shift. The small computed barrier confirms our hypothesis that the donor-acceptor interaction between the lone pair electrons of chlorine and the vacant carbon p orbital of the ketene LUMO is the key factor in stabilizing the transition state for 1,5-migration in **2**.

As for the 1,3-shift, we also calculated the barrier for the conventional pericyclic 1,5-Cl migration in 5-chloro-

1,3-pentadiene (**TS4**, Figure 3). This kind of reaction requires the movement of the chlorine atom above the molecular plane as there is no additional stabilizing effect from the orthogonal orbitals of a ketene function. The transition state (Figure 3) lies 173 kJ mol⁻¹ above the equilibrium structure.

To explain the facile 1,3- and 1,5-shifts, let us consider the orbital interactions involved. For concerted 1,3-H migration in allylic systems there exists only the antarafacial pathway, which results in high steric strain and poor orbital overlap and is hence almost unknown.19 Chart 1 depicts the orbitals involved in the normal 1,3 and 1,5-pericyclic rearrangements.

However, if the migrating atom is capable of undergoing inversion^{1,20} or if interaction with additional (orthogonal) orbitals is possible, as in the case of ketenes and other cumulenes, then the migration can also proceed via a suprafacial pathway.^{7a} Thus, for migrating groups other than hydrogen, 1,3-rearrangements become feasible, as demonstrated in Chart 2: interaction of the filled lone pair orbital of the migrating atom with the vacant central carbon p orbital of the ketene LUMO (which is perpendicular to the normal π system).

In contrast to the clearly pericyclic chlorine rearrangements in 3-chloro-1-propene and 5-chloro-1,3-pentadiene, where the chlorine migrates above the molecular planes, one can describe the in-plane 1,*n*-shifts involving ketene functions as pseudopericyclic, as there is "a disconnection (or orthogonality^{7a}) in the cyclic array of overlapping orbitals".²¹ However, the chlorine migration in ketenes may be conveniently described as a "lone pair-LUMOmediated pericyclic reaction". Note that these reactions are not subject to the normal rules¹ of orbital symmetry.

The donor-acceptor interaction in **TS3** is facilitated by the fact that both the donor and acceptor orbitals lie in the molecular plane. Thus, one would anticipate a higher barrier for systems that prohibit such a favorable orbital overlap. This is readily illustrated by the 1,5- Cl shift in 6-chlorocyclohexa-2,4-dienone (**3**, eq 4).

Hartshorn et al. have examined an analogous system

 $3a'$

 $3a$

Figure 2. TS1 for $1a \rightleftarrows 1a'$ (eq 3) and **TS2** for the 1,3-Cl migration in 3-chloro-1-propene.

Figure 3. TS3 for 1,5-Cl shift in (2-(chlorocarbonyl)vinyl)ketene and **TS4** for 1,5-Cl shift in 5-chloro-1,3-pentadiene.

Chart 2. Orbital Interactions for Lone Pair-**LUMO-Mediated Pericyclic 1,3- and 1,5-Shifts.**

with semiempirical methods.^{4b} They reported a PM3calculated barrier of 139 kJ mol⁻¹ for the rearrangement of 4,6-dichloro-2,5,6-trimethylcyclohexa-2,4-dienone to 4,6-dichloro-2,3,6-trimethylcyclohexa-2,4-dienone. We calculate 1,5-Cl migration in **3** to have a moderate barrier of 121 kJ mol-1, via transition structure **TS5** (Figure 4), which is analogous to **TS4**.

Chlorocarbonylimine-α-Chloroisocyanate Inter**conversion.** It is known that the 1,3-Cl migration in carbamoyl chlorides of type 4a to give α -chloro isocyanates (eq $\bar{5}$) is a facile process.²² In agreement with these experimental findings, our calculations of the chlorotropic equilibrium (eq 5, $\overline{R} = H$) favor the α -chloro isocyanate form **4b** by 48 kJ mol⁻¹.

Figure 4. TS5 for 1,5-Cl shift in 6-chlorocyclohexa-2,4 dienone.

The barrier for the tranformation of **4a** to **4b** via **TS6** is predicted to be 133 kJ mol⁻¹ at the G2(MP2, SVP) level of theory. Again, **TS6** turns out to be almost planar (28°, Figure 5), thus indicating another example of a lone pair-LUMO-mediated pericyclic reaction.

Semiempirical Calculations. Both semiempirical methods predict the *s-cis* isomer of α -oxo ketene 1 to be more stable, in contrast to the ab initio results. PM3 favors **1b** by 7 kJ mol⁻¹, AM1 only by little more than 1 kJ mol⁻¹. AM1 clearly overestimates the activation barrier associated with the 1,3-rearrangement (88 kJ mol-¹ (19) (a) Jensen, F. *J. Am. Chem. Soc.* **¹⁹⁹⁵**, *¹¹⁷*, 7487 and references). PM3, however, predicts the transition state **TS1**

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TS6

Figure 5. TS6 for the chlorotropic equilibrium $4a \rightleftharpoons 4b$.

to be 51 kJ mol-¹ above the *s-trans* oxo ketene in very good agreement with the G2(MP2,SVP) result.

Conformer **2a** is calculated to be the least stable isomer using both semiempirical models. However, AM1 gives a better description of the energetic distribution of the remaining seven isomers than does PM3. Again, the AM1-predicted activation barrier is too high, whereas PM3 tends to slightly underestimate the energy of the transition state.

The activation energy for isomerization of **3a** is determined to be 155 (PM3) or 190 kJ mol⁻¹ (AM1), again showing a better agreement with the ab initio results for PM3.

The same is true for the chlorotropic equilibrium **4a** \rightleftharpoons **4b**. PM3 reproduces the ab initio calculated barrier very well (138 kJ mol⁻¹), while AM1 is again too high $(162 \text{ kJ mol}^{-1}).$

In general, PM3 seems to be the more reliable semiempirical method for the prediction of activation barriers in the examples presented here.

Conclusions

The 1,3-Cl shifts in α -oxo ketenes (eqs 1 and 3), the vinylogous 1,5-Cl shifts in (2-(chlorocarbonyl)vinyl)ketene (eq 2) and the 1,3-Cl shift interconverting (chlorocarbonyl)imine and chloromethyl isocyanates (eq 5) are dramatically accelerated in comparison with conventional pericyclic 1,3- and 1,5-shifts of Cl. These facile chlorine shifts are mediated by a favorable in-plane interaction between a filled chlorine lone pair orbital and a vacant carbon p orbital on the ketene or isocyanate moiety. It may be expected that this principle of lone pair-LUMOmediated pericyclic reaction applies also to the migration of other halogens (particularly Br) and other cumulenes.

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